





- MASS nouns don't take plural marking (except with kind reading) and do not combine with plain numerals but with measure phrases. E.g. *watter*, *wood*, *furniture*. Denotations of predicates built on mass nouns:

$$(15) \quad \llbracket \text{water} \rrbracket = \{ \dots, a, b, c, a+b, a+c, b+c, a+b+c \}$$

$$(16) \quad \llbracket \text{two liters of water} \rrbracket = \text{e.g. } \{ a, b+c \}$$

- Formal properties for 1-place nominal predicates:

(17) A predicate P is **QUANTIZED** iff  $\forall x \forall y [ P(x) \wedge P(y) \rightarrow \neg(y \subset x) ]$   
That is, a predicate P is quantized iff: for any individuals x and y in its denotation, one individual cannot possibly be a proper part of the other. (Krifka 1989: D14 QUA)

(18) A predicate P is **CUMULATIVE** iff  $\exists x \exists y [ P(x) \wedge P(y) \wedge x \neq y ] \wedge \forall x \forall y [ P(x) \wedge P(y) \rightarrow P(x+y) ]$   
That is, a predicate P is cumulative iff: there are at least two different individuals in its denotation and, for any x and y in its denotation, the sum x+y will also be in its denotation. (Krifka 1989: D13 SCUM)

**QUESTION 4:** Which of the nominal predicates in (12)-(16) are quantized and which are cumulative?

**QUESTION 5:** It is clear that a given predicate P cannot be at the same time quantized and cumulative. But can a predicate be neither quantized nor cumulative? In other words, are the notions in (17)-(18) contrary opposites (like *hot* and *cold*) or contradictory opposites (like *hot* and *not hot*)? Explain.

### 3. The domain of events.

- We want to explain the impact of the shape of the direct object in aspectual composition; more concretely, we want to explain the pattern below:

- (19) a. Kate ate an apple / two apples.  $\Rightarrow$  **TELIC**  
b. Kate ate apples.  $\Rightarrow$  **ATELIC**
- (20) a. John pushed a cart / two carts.  $\Rightarrow$  **ATELIC**  
b. John pushed carts.  $\Rightarrow$  **ATELIC**

- Formal properties for 1-place verbal predicates (same as (17)-(18) but for events):

(21) A predicate Q is **QUANTIZED** iff  $\forall e \forall e' [ Q(e) \wedge Q(e') \rightarrow \neg(e' \subset e) ]$

(22) A predicate Q is **CUMULATIVE** iff  $\exists e \exists e' [ P(e) \wedge P(e') \wedge e \neq e' ] \wedge \forall e \forall e' [ P(e) \wedge P(e') \rightarrow P(e+e') ]$

- Formal properties for 2-place  $\theta$ -role predicates combining with an individual and an event:

(23) A predicate R is **SUMMATIVE** iff

$$\forall e \forall e' \forall x \forall x' [ R(e,x) \wedge R(e',x') \rightarrow R(e+e', x+x') ]$$

[= Basically, the 2-place version of cumulative.]

E.g., two events e and e' of drinking a glass of wine yield an event e+e' of drinking two glasses of wine. (Krifka 1989: D29)

(24) A predicate R satisfies **MAPPING TO OBJECTS** iff

$$\forall e \forall e' \forall x [ R(e,x) \wedge e' \subset e \rightarrow \exists x' [x' \subset x \wedge R(e',x')] ]$$

E.g. every proper subpart of an event e of drinking a glass of wine corresponds to a proper subpart of the glass of wine.<sup>1</sup> (Krifka 1989: D32)

(25) A predicate R satisfies **UNIQUENESS OF OBJECTS** iff

$$\forall e \forall x \forall x' [ R(e,x) \wedge R(e,x') \rightarrow x=x' ]$$

That is, an event is related to a specific object. E.g., a drinking of a glass of wine is related only to this glass of wine as a theme/patient and to nothing else. (Krifka: D30)

- Semantic representation of the VP-predicates under consideration:

(26)  $\llbracket \textit{eat two apples} \rrbracket = \lambda e. \exists x [ \textit{eat}(e) \wedge \textit{two-apples}(x) \wedge \textit{theme}(e,x) ]$

(27)  $\llbracket \textit{eat apples} \rrbracket = \lambda e. \exists x [ \textit{eat}(e) \wedge \textit{apples}(x) \wedge \textit{theme}(e,x) ]$

(28)  $\llbracket \textit{push two carts} \rrbracket = \lambda e. \exists x [ \textit{push}(e) \wedge \textit{two-carts}(x) \wedge \textit{theme}(e,x) ]$

(29)  $\llbracket \textit{push carts} \rrbracket = \lambda e. \exists x [ \textit{push}(e) \wedge \textit{carts}(x) \wedge \textit{theme}(e,x) ]$

(30) Template  $\phi$ :  $\lambda e. \exists x [ Q(e) \wedge P(x) \wedge R(e,x) ]$

- In what cases will the resulting VP-predicate be CUMULATIVE?

(30) If the verbal predicate Q is cumulative, the direct object predicate P is cumulative and the theta-predicate R is summative, then the resulting VP-predicate  $\phi$  will be cumulative.

(32) Proof: (Krifka 1989: 93)

We want to prove that  $\phi$  is cumulative when so composed; that is, we want to prove that if  $\phi(e_1)$  and  $\phi(e_2)$ , then  $\phi(e_1+e_2)$ .

Assume e1 and e2 for which  $\phi(e_1)$  and  $\phi(e_2)$ . According to the definition of  $\phi$ , there are two objects x1 and x2 such that  $[Q(e_1) \wedge P(x_1) \wedge R(e_1,x_1)]$  and  $[Q(e_2) \wedge P(x_2) \wedge R(e_2,x_2)]$ . Since Q and P are cumulative, it holds that  $Q(e_1+e_2)$  and  $P(e_1+e_2)$ . Since R is summative, it holds that  $R(e_1+e_2, x_1+x_2)$ . Putting all the pieces together, it holds that  $[Q(e_1+e_2) \wedge P(x_1+x_2) \wedge R(e_1+e_2, x_1+x_2)]$ . Given this, it follows that  $\phi(e_1+e_2)$ , that is, it follows that  $\exists x [Q(e_1+e_2) \wedge P(x) \wedge R(e_1+e_2,x)]$ , where  $x = x_1+x_2$ .

<sup>1</sup> Modified from Krifka: instead of  $\subset$ , we have  $\subset$ . See also Bhatt and Pancheva (2005).

- Quantized P**
- (33)  $\llbracket \textit{eat two apples} \rrbracket = \lambda e. \exists x [ \textit{eat}(e) \wedge \textit{two-apples}(x) \wedge \textit{theme}(e,x) ] \Rightarrow$  **NOT CUMUL.**
- (34)  $\llbracket \textit{eat apples} \rrbracket = \lambda e. \exists x [ \textit{eat}(e) \wedge \textit{apples}(x) \wedge \textit{theme}(e,x) ] \Rightarrow$  **CUMULATIVE**
- (35)  $\llbracket \textit{push two carts} \rrbracket = \lambda e. \exists x [ \textit{push}(e) \wedge \textit{two-carts}(x) \wedge \textit{theme}(e,x) ] \Rightarrow$  **NOT CUMUL.**
- (36)  $\llbracket \textit{push carts} \rrbracket = \lambda e. \exists x [ \textit{push}(e) \wedge \textit{carts}(x) \wedge \textit{theme}(e,x) ] \Rightarrow$  **CUMULATIVE**
- Cumulative P**
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■ In what cases will the resulting VP-predicate be QUANTIZED?

Note: we leave aside iterative interpretations.

(37) If the direct object predicate P is quantized and the theta-predicate R satisfies Mapping to Objects and Uniqueness of Objects, then the resulting VP-predicate  $\phi$  will be quantized.

(38) Proof: (Krifka 1989: 95)

We assume to the contrary that P is quantized but that the resulting  $\phi$  is not, that is, that  $\phi(e_1)$ ,  $\phi(e_2)$  and  $e_1 \subset e_2$ . We will show that this leads to a contradiction when  $\phi$  is composed as in (37).

We assume that P is quantized,  $\phi(e_1)$ ,  $\phi(e_2)$  and  $e_1 \subset e_2$ . According to the definition of  $\phi$ , there are two objects  $x_1$  and  $x_2$  such that  $[Q(e_1) \wedge P(x_1) \wedge R(e_1, x_1)]$  and  $[Q(e_2) \wedge P(x_2) \wedge R(e_2, x_2)]$ . Since  $e_1 \subset e_2$  and since R satisfies Mapping to Objects, there is an  $x_3$  for which  $x_3 \subset x_1$  and  $R(e_2, x_3)$ . Because of Uniqueness of Objects and since we already have  $R(e_2, x_2)$  and  $R(e_2, x_3)$ , it holds that  $x_2 = x_3$ . This, together with  $x_3 \subset x_1$ , entails that  $x_2 \subset x_1$ . Putting now the pieces together, we have that  $P(x_1)$ ,  $P(x_2)$  and  $x_2 \subset x_1$ . But this means that P is not quantized, which contradicts our assumption.

- Quantized P** **Mapping to Objects**
- (39)  $\llbracket \textit{eat two apples} \rrbracket = \lambda e. \exists x [ \textit{eat}(e) \wedge \textit{two-apples}(x) \wedge \textit{theme}(e,x) ] \Rightarrow$  **QUANTIZED**
- (40)  $\llbracket \textit{eat apples} \rrbracket = \lambda e. \exists x [ \textit{eat}(e) \wedge \textit{apples}(x) \wedge \textit{theme}(e,x) ] \Rightarrow$  **NOT QUANTIZ.**
- (41)  $\llbracket \textit{push two carts} \rrbracket = \lambda e. \exists x [ \textit{push}(e) \wedge \textit{two-carts}(x) \wedge \textit{theme}(e,x) ] \Rightarrow$  **NOT QUANTIZ.**
- (42)  $\llbracket \textit{push carts} \rrbracket = \lambda e. \exists x [ \textit{push}(e) \wedge \textit{carts}(x) \wedge \textit{theme}(e,x) ] \Rightarrow$  **NOT QUANTIZ.**
- Not quantized** **No Mapping to Objects**
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**QUESTION 6:** Which of the two formal properties defined for the resulting VP-predicates -- (non-)cumulative and (non-)quantized-- match the intuitive telic/atelic distinction?